

RIJKSUNIVERSITEIT GRONINGEN

**Stochasticity and Variability in the
Dynamics and Genetics of Populations**

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To Leonardo Mateu

To the Organic Intellectuals

To the Sewer Poets.

Contents

List of Figures	xiii
Samenvatting (NL)	xv
Summary (EN)	xvi
Resumen (ES)	xviii
Acknowledgements	xx
General Introduction	1
I Population Dynamics	19
1 Density Dependence as a Size-Independent Regulatory Mechanism	21
1.1 INTRODUCTION	23
1.2 “MECHANICS” OF SIZE REGULATION	25
1.3 GENERALIZED RATES OF GROWTH	30
1.4 STABILITY ANALYSES	31
1.5 SCALING LAWS	41
1.6 DISCUSSION	46

1.7	CONCLUDING REMARKS	53
2	Determinism, Noise, and Spurious Estimations in a Generalized Model of Population Growth	57
2.1	INTRODUCTION	59
2.2	DISTRIBUTION OF THE GROWTH RATES	62
2.3	DENSITY REGULATION BY NOISE	66
2.4	ESTIMATIONS OF GROWTH PATTERNS	69
2.5	CONCLUDING REMARKS	73
II	Population Genetics	75
3	Statistical Mechanics and the Evolution of Polygenic Quantitative Traits	77
3.1	INTRODUCTION	79
3.2	GENERAL ANALYSIS	84
3.3	DIRECTIONAL SELECTION, MUTATION, AND DRIFT	92
3.4	LOW MUTATION RATES: $4N\mu < 1$	107
3.5	DISCUSSION	114
4	<i>G</i> spotted in <i>Rana temporaria</i>!	121
4.1	INTRODUCTION	123
4.2	THEORETICAL BACKGROUND	125
4.3	MATERIALS AND METHODS	129
4.4	RESULTS	132
4.5	DISCUSSION	136
5	Evolution of Polygenic Traits: Adaptation at Maximal Entropy.	143
5.1	INTRODUCTION	145
5.2	MECHANISMS OF QUANTITATIVE EVOLUTION	147
5.3	ENTROPY MAXIMIZING THEORY	151

5.4	CONCLUDING REMARKS	165
6	Perspectives: Pleiotropic effects on the \mathcal{G}-matrix	169
6.1	STANDING AND MUTATIONAL VARIATION	170
6.2	SOME CONSEQUENCES OF PLEIOTROPY	175
6.3	MOVING ON WITH THE \mathcal{G} MATRIX	181
6.4	CONCLUDING REMARKS	183
7	Perspectives: The evolution of quantitative characters under stabilizing selection, mutation, and drift.	187
7.1	INTRODUCTION	188
7.2	MAX-ENTROPIC APPROACH	191
7.3	SINGLE LOCUS DYNAMICS	196
7.4	FORMULATING POLYGENIC DYNAMICS	206
7.5	POSTSCRIPT ON STABILIZING SELECTION	213
III	Synthesis	221
8	Synthesis	223
8.1	AN OVERVIEW OF THE CONCLUSIONS	224
8.2	FURTHER EVOLUTIONARY IMPLICATIONS	227
8.3	RESEARCH PERSPECTIVES	244
	Bibliography	253
A	Maximization of entropy or of mean fitness?	283
A.1	MAXIMUM ENTROPY	284
A.2	MAXIMUM FITNESS	285
B	Notes on the analogy with Statistical Mechanics in Physics	291

C	Estimations of the genetic architecture of <i>Rana temporaria</i>	297
C.1	GENETIC EFFECTS AND EFFECTIVE NUMBER OF LOCI	298
C.2	GENETIC ARCHITECTURE AND M.S.D. EQUILIBRIUM	303
C.3	PLEIOTROPIC STRUCTURES AND FITNESS DIFFERENTIALS (β)	305
C.4	EIGENSTRUCTURES OF THE \mathcal{G} MATRICES	307
D	Formulas for the quantitative variables	311
D.1	DIRECTIONAL SELECTION	312
D.2	STABILIZING SELECTION	322