

Mathematical modeling of complex systems

Microphase separation dynamics in
polymer liquids

RIJKSUNIVERSITEIT GRONINGEN

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Proefschrift
ter verkrijging van het doctoraat in de
Wiskunde en Natuurwetenschappen
aan de Rijksuniversiteit Groningen
op gezag van de
Rector Magnificus, Dr. D.F.J. Bosscher,
in het openbaar te verdedigen op
vrijdag 18 september 1998
om 13.15 uur

door

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geboren op 3 mei 1971
te Voorburg

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*Shoot for the moon. Even if you miss it,
you will land among the stars.
(Les Brown)*

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